# Fluorescence Quenching by Oxygen of 9,10-Dimethylanthracene in Liquid and Supercritical Carbon Dioxide

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The contribution of diffusion to the fluorescence quenching by oxygen of 9,10-dimethylanthracene (DMEA) in liquid CO<sub>2</sub> and supercritical CO<sub>2</sub> (SCF CO<sub>2</sub>) at pressures up to 60 MPa was investigated. For comparison, the fluorescence quenching by CBr<sub>4</sub> of DMEA was also investigated. The apparent activation volume of the quenching rate constant,  $k_q$ , was  $8 \pm 1$  and  $10 \pm 3$  cm<sup>3</sup>/mol for DMEA/O<sub>2</sub>, and  $42 \pm 7$  and  $400 \pm 90$  cm<sup>3</sup>/mol for DMEA/CBr<sub>4</sub> in liquid CO<sub>2</sub> (25 °C, 10 MPa) and SCF CO<sub>2</sub> (35 °C, 8.5 MPa), respectively. For DMEA/O<sub>2</sub>, the plots of ln  $k_q$  against ln  $\eta$ , where  $\eta$  is the solvent viscosity, showed a leveling-off with decreasing the solvent viscosity, whereas for DMEA/CBr<sub>4</sub> they were almost linear in both liquid and SCF CO<sub>2</sub>. The results, together with those of the pressure and the pressure-induced solvent viscosity dependences of  $k_q$  for DMEA/O<sub>2</sub> in *n*-alkanes (C<sub>4</sub> to C<sub>7</sub>) and for DMEA/CBr<sub>4</sub> in *n*-hexane, revealed that the quenching competes with diffusion. The contribution of diffusion to the quenching was analyzed on the basis of a kinetic model with solvent cage in which the quenching occurs. The bimolecular rate constant for the quenching in the solvent cage,  $k_{\text{bim}}$ , was  $6.0 \times 10^{10}$  and  $12 \times 10^{10}$  M<sup>-1</sup> s<sup>-1</sup> in liquid CO<sub>2</sub> (25 °C, 10 MPa) for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub>, respectively, and  $5.7 \times 10^{10}$  and  $12 \times 10^{10}$  M<sup>-1</sup> s<sup>-1</sup> in SCF CO<sub>2</sub> (35 °C, 8.5 MPa) for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub>, respectively. The pressure dependence of  $k_{\text{bim}}$  and the contribution of diffusion to the quenching solvent solvent of diffusion to the quenching solvent solvent solvent of diffusion to the quenching are discussed.

## Introduction

Because of its chemical and biological importance, the quenching by oxygen of the excited states of aromatic molecules with singlet and triplet spin multiplicities has been investigated by many workers, and often concluded to be nearly or fully diffusion-controlled.<sup>1-6</sup> In fact, the observed quenching rate constant,  $k_q$ , for the lowest excited singlet state (S<sub>1</sub>) of some aromatic molecules is ca.  $10^{10} \text{ M}^{-1} \text{ s}^{-1}$ , which is approximately equal to the rate constant,  $k_{diff}$ , for diffusion-controlled reactions in a continuum medium with viscosity,  $\eta$  (in poise), calculated by the Debye equation<sup>7,8</sup>

$$k_{\rm diff} = \frac{8RT}{\alpha\eta} \tag{1}$$

where  $\alpha$  is 2000 and 3000 for the slip and stick boundary conditions, respectively. However, the discrepancy between  $k_q$  and  $k_{diff}$  thus calculated is not small. This implies that  $k_{diff}$  is not expressed by eq 1 and/or the quenching involves the additional rate processes that compete with diffusion.

Supercritical fluids (SCF), which can dissolve many compounds, are very interesting because their physical properties such as viscosity and density change dramatically with a small increase in pressure or temperature. Therefore, many types of bimolecular reactions<sup>9–18</sup> including fluorescence quenching have been examined in SCF as solvent. Among them, the fluorescence quenching by carbon tetrabromide (CBr<sub>4</sub>) of some aromatic molecules that is believed to be diffusion-controlled was investigated and discussed mainly from the viewpoint of the local density augmentation and the local composition changes around the fluorophore molecules which arise as a result of the clustering of the solute molecules in SCF. For anthracene/ CBr<sub>4</sub>,<sup>17,18</sup> 1,2-benzanthracene/CBr<sub>4</sub>,<sup>18</sup> and perylene/CBr<sub>4</sub><sup>17</sup> in SCF CO<sub>2</sub>, the quenching was concluded to be diffusioncontrolled on the basis of the fact that the viscosity dependence of  $k_q$  is similar to that predicted by eq 1. For 9-cyanoanthracene/ CBr417 and 9,10-diphenylanthracene/CBr4,17 an enhanced fluorescence quenching at near-critical CO2 densities was observed and interpreted by the effects of the local quencher concentration augmentation.

Recently, we studied the fluorescence quenching by oxygen of 9,10-dimethylanthracene (DMEA) in *n*-alkane (C<sub>4</sub> to C<sub>7</sub>) at pressures up to 400 MPa,<sup>6</sup> and found that the quenching constant,  $k_q$ , decreases significantly with increasing pressure. The results, together with the pressure-induced viscosity dependence of  $k_q$ , revealed that the quenching is nearly diffusion-controlled. In general, the bimolecular quenching reaction must compete with the diffusion process in a solvent with low

viscosity when the energy transfer from the S<sub>1</sub> state of DMEA to oxygen has a limiting rate constant. However, no evidence was found in *n*-butane ( $\eta = 0.16$  cP at 25 °C and 3 MPa) that was the solvent with the lowest viscosity examined.<sup>6</sup> The viscosity of SCF CO<sub>2</sub> is very low near the critical density and increases steeply with increasing pressure. Therefore, SCF CO<sub>2</sub> is a suitable solvent for the study of the contribution of diffusion to the energy transfer by the collisional or exchange mechanism.

The fluorescence quenching by poly(bromoethane)s and CBr<sub>4</sub> of pyrene in methylcyclohexane at pressures up to 650 MPa has been examined.<sup>19</sup> It was found that the activation volume for  $k_q$  is negative and positive for the quenchers with low and high quenching ability, respectively. This was satisfactorily interpreted by a kinetic scheme via an encounter complex, followed by the formation of an exciplex in solvent cage, which is generally involved in the bimolecular reaction in liquid solution. The pressure dependence of the fluorescence quenching in liquid CO<sub>2</sub> that has very low viscosity ( $\eta = 0.074$  cP at 25 °C and 10 MPa and increases monotonically with increasing pressure) may give us evidence for the competition of diffusion with the energy transfer that occurs in the solvent cage. Furthermore, the comparison with the quenching in SCF CO<sub>2</sub> may lead to an understanding of the solvent cage effect.

The present work is focused on the pressure and the pressureinduced solvent viscosity dependence of the fluorescence quenching by oxygen of DMEA in both liquid and SCF CO<sub>2</sub> in order to obtain insight into the contribution of diffusion to the collisional energy transfer from the S<sub>1</sub> state of DMEA to O<sub>2</sub>. For comparison, we also studied the fluorescence quenching by CBr<sub>4</sub> of DMEA for which the quenching is concluded to be nearly or fully diffusion-controlled. From the results, together with data for fluorescence quenching by oxygen of DMEA in *n*-alkanes (C<sub>4</sub> to C<sub>7</sub>) that was previously reported,<sup>6</sup> the quenching mechanism by oxygen is discussed.

#### **Experimental Section**

9,10-Dimethylanthracene (DMEA) (Aldrich Chemical Co.) was recrystallized from methanol and then purified by thinlayer chromatography. Carbon tetrabromide (CBr<sub>4</sub>) (Wako Pure Chemicals Ltd.) of guaranteed grade was purified by sublimation twice under reduced pressure. *n*-Hexane (Merk) of spectroscopic grade and carbon dioxide (CO<sub>2</sub>) (Sumitomo Seika; purity, 99.995%) were used as received.

Fluorescence decay curve measurements at high pressure were performed by using a 0.3 ns pulse from a PRA LN103 nitrogen laser for excitation. The fluorescence intensities were measured by a Hamamatsu R1635-02 photomultiplier through a Ritsu MC-25NP monochromator and the resulting signal was digitized by using a LeCroy 9362 digitizing oscilloscope. All data were analyzed by using a NEC 9801 microcomputer, which was interfaced to the digitizer. The associated high-pressure techniques have been described in detail elsewhere.<sup>20</sup>

The sample solution of DMEA in liquid and SCF CO<sub>2</sub> with oxygen was prepared as follows. An appropriate volume of a *n*-hexane stock solution of DMEA was placed into a high-pressure cell with four optical sapphire windows. The solvent was evaporated and the high-pressure cell was evacuated, and then filled with CO<sub>2</sub> from a high-pressure syringe pump (500 MPa). The oxygen concentration was determined by introducing a known pressure of synthesized air (oxygen/nitrogen/ argon = 21/78/1 vol %, Taiyo Oxygen Co.) into the high-pressure cell. The concentration of DMEA for the fluorescence lifetime measurements was less than 0.1 in absorbance (1 cm-cell) at



**Figure 1.** Plots of  $1/\tau$  against the concentration of oxygen, [O<sub>2</sub>], in (a) SCF CO<sub>2</sub> at 35 °C and (b) liquid CO<sub>2</sub> at 25 °C.

maximum absorption wavelength in order to minimize the reabsorption effects. Sample solutions of DMEA with  $CBr_4$  were prepared by a similar procedure. Complete dissolution of oxygen and  $CBr_4$  in liquid and SCF CO<sub>2</sub> was checked by measuring the fluorescence lifetime of DMEA as a function of time.

Temperature was controlled at  $25 \pm 0.2$  and  $35 \pm 0.2$  °C. Pressure was measured by Nagano Keiki Seisakusho KH15 (68.6 MPa) and Minebea NS100A (49.0 MPa) strain gauges for the experiments in liquid CO<sub>2</sub> and SCF CO<sub>2</sub>.

## Results

Fluorescence quenching was examined in the absence and presence of the quencher (Q: oxygen and CBr<sub>4</sub>) in SCF CO<sub>2</sub> at 35 °C, and in liquid CO<sub>2</sub> and *n*-hexane at 25 °C. The decay curves were satisfactorily analyzed by a single-exponential function in all the conditions examined. The lifetimes in the absence of the quencher,  $\tau_f^0$ , were found to be 16.7 ± 0.3 and 15.5 ± 0.3 ns in liquid CO<sub>2</sub> (25 °C, 10 MPa) and SCF CO<sub>2</sub> (35 °C, 8.5 MPa), respectively. They are close to those in *n*-alkanes (C<sub>4</sub> to C<sub>7</sub>) and methylcyclohexane at 25 °C and 0.1 MPa (13.8–15.0 ns).<sup>6</sup> The lifetimes were found to be nearly independent of pressure; they were 16.1 ± 0.3 and 16.5 ± 0.3 ns at a pressure of 60 MPa in liquid CO<sub>2</sub> at 25 °C and SCF CO<sub>2</sub> at 35 °C, respectively.

The quenching rate constant,  $k_q$ , was determined using eq 2.

$$1/\tau_{\rm f} - 1/\tau_{\rm f}^{\ 0} = k_{\rm g}[Q]$$
 (2)

where  $\tau_f$  represents the fluorescence lifetime in the presence of the quencher. The plots of  $1/\tau_f$  against the concentration of oxygen in SCF and liquid CO<sub>2</sub> are shown in Figure 1. Figure 2 also shows the plots of  $1/\tau_f$  against the concentration of CBr<sub>4</sub> in SCF and liquid CO<sub>2</sub>. The values of  $k_q$  were determined from the least-squares slopes of these plots according to eq 2, and the pressure dependence of  $k_q$  is shown in Figures 3 and 4 for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub>, respectively. For DMEA/O<sub>2</sub> (Figure 3), the quenching rate constant,  $k_q$ , decreases monotonically in the whole pressure range examined, whereas for DMEA/ CBr<sub>4</sub> (Figure 4) it steeply decreases at the lower pressure region and then gradually decreases with further increase in pressure in both liquid and SCF CO<sub>2</sub>. The apparent activation volumes



**Figure 2.** Plots of  $1/\tau$  against the concentration of carbon tetrabromide, [CBr<sub>4</sub>], in (a) SCF CO<sub>2</sub> at 35 °C and (b) liquid CO<sub>2</sub> at 25 °C.



**Figure 3.** Pressure dependence of  $k_q$  for DMEA/O<sub>2</sub> in SCF CO<sub>2</sub> at 35 °C and liquid CO<sub>2</sub> at 25 °C. The solid lines were drawn by assuming that ln  $k_q = A + BP$ . The arrow indicates the pressure corresponding to the critical density at 35 °C.



**Figure 4.** Pressure dependence of  $k_q$  for DMEA/CBr<sub>4</sub> in SCF CO<sub>2</sub> at 35 °C and liquid CO<sub>2</sub> at 25 °C. The solid lines were drawn assuming that ln  $k_q = A + BP + CP^2$ . In SCF CO<sub>2</sub>, the best-fit curve was calculated in the pressure range from 8.5 to 15 MPa. The arrow indicates the pressure corresponding to the critical density at 35 °C.

for  $k_q$ ,  $\Delta V_q^{\dagger}$ , evaluated by eq 3, are listed in Table 1.

$$RT(\partial \ln k_{\rm q}/\partial P)_T = -\Delta V_{\rm q}^{\,\pm} \tag{3}$$

It is noted in Table 1 that  $\Delta V_q^{\ddagger}$  is approximately independent of the solvents for DMEA/O<sub>2</sub> whereas it strongly depends on

TABLE 1: Activation Volumes (cm<sup>3</sup>/mol) for  $k_q$ ,  $\Delta V_q^{\dagger}$ , and the Solvent Viscosity,  $\eta$ ,  $\Delta V_{\eta}^{\dagger}$ 

	DMEA/O <sub>2</sub>			DMEA/CBr <sub>4</sub>		
	liq $CO_2^a$	<i>n</i> -hexane <sup>b</sup>	SCF $CO_2^c$	liq $CO_2^a$	<i>n</i> -hexane <sup>b</sup>	SCF CO <sub>2</sub> <sup>c</sup>
$\Delta V_q^{\ddagger} \Delta V_\eta^{\ddagger}$	$\begin{array}{c} 8\pm1\\ 79\pm9\end{array}$	$11.1 \pm 0.2^d$ $23 \pm 1$	$\begin{array}{c} 10\pm3\\ 700\pm70 \end{array}$	$\begin{array}{c} 42\pm7\\ 79\pm9\end{array}$	$\begin{array}{c} 14.1\pm0.8\\ 23\pm1\end{array}$	$400 \pm 90 \\ 700 \pm 70$

 $^a$  At 10 MPa and 25 °C.  $^b$  At 0.1 MPa and 25 °C.  $^c$  At 8.5 MPa and 35 °C.  $^d$  Reference 6.



**Figure 5.** Plots of  $\ln k_q$  against  $\ln \eta$  for DMEA/O<sub>2</sub> in SCF CO<sub>2</sub> at 35 °C, and in liquid CO<sub>2</sub> and *n*-alkanes at 25 °C. The arrow indicates the value of  $\ln \eta$  at the critical density and 35 °C.

the solvents for DMEA/CBr<sub>4</sub>. Since the fluorescence quenching by oxygen and CBr<sub>4</sub> of DMEA is diffusion-controlled in nature, the activation volume,  $\Delta V_q^{\dagger}$ , was compared with that for the solvent viscosity,  $\Delta V_{\eta}^{\dagger}$ , which was evaluated from the viscosity data<sup>21–26</sup> and is also listed in Table 1. The values of the ratio of  $\Delta V_q^{\dagger}$  to  $\Delta V_{\eta}^{\dagger}$  may give a crude estimate of the contribution of diffusion to the quenching; they are ca. 0.1, 0.5, and 0.01 for DMEA/O<sub>2</sub>, and 0.5, 0.6, and 0.6 for DMEA/CBr<sub>4</sub> in liquid CO<sub>2</sub>, *n*-hexane, and SCF CO<sub>2</sub>, respectively. Thus, for DMEA/ O<sub>2</sub> in SCF CO<sub>2</sub>, the contribution of diffusion is small, suggesting that the quenching is nearly independent of the solvent viscosity, that is, pressure, but for the other systems examined, there is a significant contribution of diffusion to the quenching.

For the fluorescence quenching with a nearly diffusioncontrolled rate, a fractional power dependence of  $k_q$  on  $\eta$ , which is given by eq 4, has often been observed.<sup>5</sup>

$$k_{\rm q} = A \eta^{-\beta} \tag{4}$$

In eq 4, A is a constant that is dependent on temperature, T, but independent of pressure, and  $\beta$  is less than unity. Figure 5 shows the plots of  $\ln k_q$  against  $\ln \eta$  for DMEA/O<sub>2</sub> in SCF CO<sub>2</sub> at 35 °C and liquid CO<sub>2</sub> at 25 °C, together with the data in *n*-alkanes (C<sub>4</sub> to C<sub>7</sub>) at 25 °C.<sup>6</sup> The plot of ln  $k_q$  and ln  $\eta$  shows slightly downward curvature in liquid *n*-alkanes. The mean values of  $\beta$ were 0.59, 0.64, 0.71, and 0.64 in *n*-butane, *n*-pentane, *n*-hexane, and *n*-heptane, respectively, in the pressure range examined;<sup>6</sup> they increased to 0.74, 0.77, and 0.79 in n-pentane, n-hexane, and n-heptane, respectively, at pressures above 300 MPa. In liquid CO<sub>2</sub>, the plot of  $\ln k_q$  and  $\ln \eta$  levels off with decreasing the solvent viscosity, and the leveling-off is clearly observed in SCF  $CO_2$  (see Figure 5). These results suggest that the fluorescence quenching of DMEA by oxygen competes with but is significantly smaller than the diffusion rate in the lower solvent viscosity range.

For DMEA/CBr<sub>4</sub>, as seen in Figure 6, the plot of ln  $k_q$  against ln  $\eta$  shows slightly downward curvature in *n*-hexane as observed for DMEA/O<sub>2</sub> in *n*-alkanes; the mean value of  $\beta$  was 0.83 ± 0.02 in the whole pressure range examined and 0.93 ± 0.04 at



**Figure 6.** Plots of  $\ln k_q$  against  $\ln \eta$  for DMEA/CBr<sub>4</sub> in SCF CO<sub>2</sub> at 35 °C, and in liquid CO<sub>2</sub> and *n*-alkanes at 25 °C. The arrow indicates the value of  $\ln \eta$  at the critical critical density and 35 °C.

pressures above 300 MPa. In liquid and SCF CO<sub>2</sub>, the plot of ln  $k_q$  against ln  $\eta$  is almost linear (see Figure 6) and the values of  $\beta$  were 0.84  $\pm$  0.04 (SCF CO<sub>2</sub>) and 0.71  $\pm$  0.02 (liquid CO<sub>2</sub>). Thus, the value of  $\beta$  for DMEA/CBr<sub>4</sub> is close to unity compared to that for DMEA/O<sub>2</sub>. From the results, together with the findings for DMEA/O<sub>2</sub>, it may be concluded that the fluorescence quenching of DMEA by oxygen competes with diffusion in the whole pressure range examined and probably is only slightly slower than the diffusion rate in the lower viscosity range.

## Discussion

**Rate Constant for Diffusion**,  $k_{\text{diff}}$ . In general, when the transient terms can be neglected, the rate constant,  $k_{\text{diff}}$ , for the bimolecular diffusion-controlled reaction between the S<sub>1</sub> state of M, <sup>1</sup>M\*, and quencher, Q, is given by eq 5 in a solvent with the relative diffusion coefficient,  $D_{M^*Q}$  (= $D_{M^*} + D_Q$ ):<sup>7.8</sup>

$$k_{\rm diff} = 4\pi r_{\rm M*Q} D_{\rm M*Q} N_{\rm A} / 10^3$$
 (5)

where  $r_{M^*Q}$  and  $N_A$  are the encounter distance and Avogadro's number, respectively. The relationship between  $D_i$  ( $i = M^*$  or Q) and  $\zeta_i$ , the friction coefficient, for the solute molecule, i, in a given solvent is expressed by the Einstein equation,  $D_i = k_B T/$  $\zeta_i$ , where  $k_B$  is the Boltzmann constant. Since the hydrodynamic friction,  $\zeta_i^H$ , for a solute molecule of spherical radius,  $r_i$ , in a continuum medium with viscosity,  $\eta$ , is given by  $\zeta_i^H = f_i \pi r_i \eta$ (Stokes' law), one can obtain the Stokes–Einstein (SE) equation

$$D_i^{\rm SE} = k_{\rm B} T / f_i \pi r_i \eta \tag{6}$$

where  $f_i = 4$  and 6 for the slip and stick boundary limits, respectively. However, the SE equation has been often observed to break down for diffusion in liquid and SCF solutions.<sup>7,27–29</sup>

In the previous publications,  $^{19,30,31}$  the solvent-viscosity dependence of  $k_{\text{diff}}$  induced by pressure was described successfully for several quenching systems on the basis of an empirical equation proposed by Spernol and Wirtz.<sup>2,32,33</sup> According to their approach, the diffusion coefficient,  $D_t^{SW}$ , is expressed by

$$D_i^{\rm SW} = k_{\rm B} T / 6\pi f_i^{\rm SW} r_i \eta \tag{7}$$

where  $f_i^{SW}$  represents a microfriction factor and is given by

$$f_i^{\rm SW} = (0.16 + 0.4r_i/r_{\rm S})/(0.9 + 0.4T_{\rm S}^{\rm r} - 0.25T_i^{\rm r}) \quad (8)$$

In eq 8, the first parenthetical quantity depends only on the solute-to-solvent size ratio  $(r_i/r_S)$ . The second parenthetical quantity involves the reduced temperatures,  $T_S^r$  and  $T_i^r$ , of

TABLE 2: Values of van der Waals Radii,  $r_W$ , of the Solvents and  $\alpha^{SW}(trunc)$ 

		$\alpha^{SW}(trunc)$		
	<i>r</i> <sub>W</sub> <sup><i>a</i></sup> /nm	DMEA/O <sub>2</sub>	DMEA/CBr <sub>4</sub>	
$CO_2$	0.200	1540	2360	
<i>n</i> -butane	0.267	1263	1890	
<i>n</i> -pentane	0.285	1211	1800	
n-hexane	0.301	1171	1730	
<i>n</i> -heptane	0.315	1137	1670	

 $^{\it a}$  Estimated by the method of Bondi.  $^{34}$  The values of  $r_W$  were evaluated to be 0.173, 0.289, and 0.365 nm for O\_2, CBr\_4, and DMEA, respectively.

solvent and solute, respectively, which can be calculated by using the melting point,  $T_{mp}$ , and boiling point,  $T_{bp}$ , of the solvent or solute at the experimental temperature, T, according to

$$T_{iS}^{r} = [T - T_{mp(S)}] / [T_{bp(S)} - T_{mp(S)}]$$
(9)

From the approximation by Spernorl and Wirtz, eq 10 can be derived

$$k_{\rm diff} = \frac{2RTr_{\rm M^{*}Q}}{3000\eta} \left( \frac{1}{f_{\rm M^{*}}^{\rm SW} r_{\rm M^{*}}} + \frac{1}{f_{\rm Q}^{\rm SW} r_{\rm Q}} \right)^{-1}$$
(10)

By comparing with eq 1,  $\alpha^{SW}$  is given by

$$\alpha^{\rm SW} = \frac{1.2 \times 10^4}{r_{\rm M^*Q}} \left( \frac{1}{f_{\rm M^*}^{\rm SW} r_{\rm M^*}} + \frac{1}{f_{\rm Q}^{\rm SW} r_{\rm Q}} \right)^{-1}$$
(11)

The values of  $f_i^{SW}$ (full) and  $f_i^{SW}$ (trunc) can be evaluated by eq 8 and by neglecting the second parenthetical quantity in eq 8, respectively.<sup>2</sup> In this study, we evaluated  $f_i^{SW}$ (trunc) alone since  $f_i^{SW}$ (full) for the oxygen-solvent systems gives a negative value. In the calculation of  $f_i^{SW}$ (trunc), the values of the radii,  $r_w$ , of the solute and solvent molecules listed in Table 2 were used. The values of  $\alpha^{SW}(trunc)$  thus calculated by eq 11 for the quenching systems studied in this work are shown in Table 2. It is noted in Table 2 that  $\alpha^{SW}$ (trunc) are close to the value for slip boundary limit ( $\alpha = 2000$ ) for DMEA/CBr<sub>4</sub> in *n*-hexane and CO<sub>2</sub>. However, for DMEA/O<sub>2</sub>,  $\alpha^{SW}$ (trunc) is significantly smaller than the value for the slip boundary limit; it seems to decrease with decreasing radius of the solvent molecule. This may be attributed to the large difference in the size of DMEA and O<sub>2</sub> as predicted by the first parenthetical quantity in eq 8.

**Quenching in Liquid Solution.** In the present work, we measured the pressure dependence of the fluorescence quenching constant,  $k_q$ , for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub> in both liquid and SCF CO<sub>2</sub>, and also that for DMEA/CBr<sub>4</sub> in *n*-hexane. In this section, we first discuss the contribution of diffusion to the quenching for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub> in liquid solution by comparing the result for DMEA/CBr<sub>4</sub> with that for DMEA/O<sub>2</sub> reported previously.<sup>6</sup> Then, we discuss the results obtained in SCF CO<sub>2</sub>.

For the fluorescence quenching by heavy-atom quencher (Q) of pyrene  $({}^{1}M^{*})$  in liquid solution, the quenching occurs via an exciplex (MQ)\* which is formed from an encounter complex  $({}^{1}M^{*}Q)_{en}$  between  ${}^{1}M^{*}$  and Q in the solvent cage as in Scheme 1,  ${}^{19}$  where the bar indicates the solvent cage. Although there is no evidence of the exciplex formation between oxygen and the S<sub>1</sub> state of DMEA, Scheme 1 also may be applied to the present systems under considerations since both of the quenching systems should be kinetically interpreted in the same



**Figure 7.** Plots of  $\gamma/k_q$  against  $\gamma\eta$  for DMEA/O<sub>2</sub> in *n*-alkane, and for DMEA/CBr<sub>4</sub> in *n*-hexane at 25 °C.

## **SCHEME 1**



framework. Based on Scheme 1, the observed rate constant,  $k_q$ , is given by

$$k_{\rm q} = \frac{k_{\rm -diff}}{1 + k_{\rm -diff} \left( \frac{k_{\rm p} + k_{\rm -c}}{k_{\rm c} k_{\rm p}} \right)}$$
(12)

When the rate constant for diffusion,  $k_{\text{diff}}$ , is expressed by eq 1 ( $\alpha$  is replaced by  $\alpha^{\text{ex}}$ ), one may derive eq 13 from eqs 1 and 12.

$$\frac{1}{k_{\rm q}} = \left(\frac{k_{\rm p} + k_{\rm -c}}{k_{\rm c}k_{\rm p}}\right) \left(\frac{k_{\rm -diff}}{k_{\rm diff}}\right) + \frac{\alpha^{\rm ex}}{8RT}\eta$$
(13)

In eq 13, the pressure dependence of  $k_{\text{diff}}/k_{-\text{diff}}$  is assumed to be given by that of the radial distribution function,  $g(r_{\text{M}*\text{Q}})$ , at the closest approach distance (the encounter distance),  $r_{\text{M}*\text{Q}}$ ( $=r_{\text{M}*} + r_{\text{Q}}$ ) with hard spheres.<sup>19</sup> By using this relation, eq 14 is derived and successfully applied to the fluorescence quenching by the heavy-atom quenchers with a nearly diffusion-controlled rate.<sup>19</sup>

$$\frac{\gamma}{k_{\rm q}} = \left(\frac{k_{\rm p} + k_{\rm -c}}{k_{\rm c}k_{\rm p}}\right) \left(\frac{k_{\rm -diff}}{k_{\rm diff}}\right)_0 + \frac{\alpha^{\rm ex}}{8RT} \gamma \eta \tag{14}$$

where  $\gamma$  is the ratio of  $g(r_{M^*Q})$  at *P* MPa to that at a reference pressure,  $P_0$  MPa,  $g(r_{M^*Q})_P/g(r_{M^*Q})_0$ , and  $(k_{-diff}/k_{diff})_0$  is  $k_{-diff}/k_{diff}$  at  $P_0$  MPa.<sup>35</sup> According to eq 14, the plot of  $\gamma/k_q$  against  $\gamma\eta$  should be linear when  $(k_p + k_{-c})/(k_c k_p)$  is independent of pressure.

The plot of  $\gamma/k_q$  against  $\gamma\eta$  for DMEA/O<sub>2</sub> in *n*-alkanes (C<sub>4</sub> to C<sub>7</sub>) and also for DMEA/CBr<sub>4</sub> in *n*-hexane is shown in Figure 7. The plot of  $\gamma/k_q$  against  $\gamma\eta$  for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub> in liquid CO<sub>2</sub> is also shown in Figure 8a. All the plots shown in Figures 7 and 8a are approximately linear with positive intercepts, indicating that the quenching competes with diffusion, and hence  $(k_p + k_{-c})/k_c k_p$  is approximately independent of  $\eta\gamma$ , that is, pressure. These observations are consistent with those found for the fluorescence quenching by polybromomethanes



**Figure 8.** Plots of  $\gamma/k_q$  against  $\gamma\eta$  for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub> in (a) liquid CO<sub>2</sub> at 25 °C and (b) SCF CO<sub>2</sub> at 35 °C.

TABLE 3: Values of  $\alpha^{ex}$  and  $k_{bim}^0$  for DMEA/O<sub>2</sub> in SCF CO<sub>2</sub> at 35 °C, and in Liquid CO<sub>2</sub> and *n*-Alkanes at 25 °C

	DMEA/O <sub>2</sub>		DMEA/CBr <sub>4</sub>		
	av	$k_{\rm bim}^{0/}$	av	$k_{\rm bim}^{0/}$	
solvent	$\alpha^{ex}$	$10^{10} \text{ M}^{-1} \text{ s}^{-1}$	$\alpha^{cx}$	10 <sup>10</sup> M <sup>1</sup> S <sup>1</sup>	
SCF CO <sub>2</sub>	$3500\pm300$	$5.7 \pm 0.9^{a}$	$5800\pm200$	$12 \pm 4^{a}$	
liquid CO <sub>2</sub>	$3100\pm100$	$6.0 \pm 0.2^b$	$5200\pm200$	$12 \pm 2^{b}$	
<i>n</i> -butane	$1480 \pm 30$	$8.5\pm0.7^{c}$			
<i>n</i> -pentane	$940 \pm 20$	$5.6\pm0.9^d$			
<i>n</i> -hexane	$940 \pm 20$	$5.4 \pm 0.8^d$	$1820 \pm 30$	$5.5 \pm 0.9^{d}$	
<i>n</i> -heptane	$690 \pm 40$	$3.6 \pm 0.9^{d}$			

 $^a$  At 8.5 MPa and 35 °C.  $^b$  At 10 MPa and 25 °C.  $^c$  At 3.0 MPa and 25 °C.  $^d$  At 0.1 MPa and 25 °C.

of pyrene in methylcyclohexane.<sup>19</sup> The values of  $\alpha^{ex}$  and the bimolecular rate constant,  $k_{bim}^0$ , defined by eq 15

$$k_{\rm bim}^{\ 0} = \left(\frac{k_{\rm p}k_{\rm c}}{k_{\rm p} + k_{\rm -c}}\right) \left(\frac{k_{\rm -diff}}{k_{\rm diff}}\right) \tag{15}$$

were determined from the least-squares intercept and slope of the plots (Figures 7 and 8) and are summarized in Table 3. For DMEA/O<sub>2</sub>,  $\alpha^{ex}$  is nearly equal to  $\alpha^{SW}$ (trunc) in *n*-butane, *n*-pentane, and *n*-hexane, whereas it is significantly larger than that in liquid CO<sub>2</sub>. For DMEA/CBr<sub>4</sub>,  $\alpha^{ex}$  is nearly equal to  $\alpha^{SW}$ -(trunc) in *n*-hexane, but one can also see large discrepancy between  $\alpha^{ex}$  and  $\alpha^{SW}$ (trunc) in liquid CO<sub>2</sub> as found for DMEA/ O<sub>2</sub>.

In the previous work,<sup>19,30,31</sup> we showed that  $\alpha^{ex}$  is well described by  $\alpha^{SW}$  for the heavy-atom quenching of fluorescence of pyrene in liquid solution. In this work,  $\alpha^{SW}$ (trunc) also gives good approximation to  $\alpha^{ex}$  for DMEA/CBr<sub>4</sub> in *n*-hexane and for DMEA/O<sub>2</sub> in *n*-alkanes (C<sub>4</sub> to C<sub>6</sub>) except for *n*-heptane. However,  $\alpha^{ex}$  is about 2 times larger than  $\alpha^{SW}$ (trunc) in liquid CO<sub>2</sub> for both of the quenching systems. The microfriction factor,  $f_i^{SW}$  given by eq 8 involves the solute–solvent interactions as well as the solute-to-solvent size ratio. Hence, it seems likely that the expression of  $f_i^{SW}$  (eq 8) cannot be applied for DMEA/ O<sub>2</sub> and DMEA/CBr<sub>4</sub> in liquid CO<sub>2</sub>. That is, for these systems, larger  $f_i^{SW}$  (*i* = DMEA, O<sub>2</sub>, and CBr<sub>4</sub>), which may arise as results of stronger solute–solvent interactions and/or larger



**Figure 9.** Pressure dependence of  $k_{\text{diff}}(\bigcirc)$ ,  $k_{\text{bin}}(\bigoplus)$ ,  $k_q(\triangle)$ , and  $k_q(\text{cal})$ ( $\bigtriangledown$ ) for DMEA/O<sub>2</sub> in (a) SCF CO<sub>2</sub> at 35 °C, (b) liquid CO<sub>2</sub>, and (c) *n*-hexane at 25 °C.

contribution of the solute-solvent size ratio as compared to those predicted by eq 8, might be expected although the  $1/\eta$  dependence of  $k_{\text{diff}}$  is still valid.

Quenching in SCF CO<sub>2</sub>. The plot of  $\gamma/kq$  against  $\gamma\eta$  for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub> in SCF CO<sub>2</sub> is shown in Figure 8b. The plots shown in Figure 8b are approximately linear with positive intercepts, meaning that the quenching competes with diffusion and hence  $(k_p + k_{-c})/k_c k_p$  is approximately independent of  $\gamma\eta$ , that is, pressure. These observations are consistent with those found in liquid solutions described in the previous section. The values of  $\alpha^{ex}$  and the bimolecular rate constant,  $k_{bim}^{0}$  (eq 15), which were determined from the least-squares slope and intercept of the plots shown in Figure 8b, respectively, are listed in Table 3, together with those in liquid solutions. It is noted in Table 3 that the values of  $k_{\text{bim}}^0$  in SCF CO<sub>2</sub> (35 °C, 8.5 MPa) are approximately equal to those in liquid CO<sub>2</sub> (25 °C, 10.0 MPa) for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub>, respectively. It is also noted that the value of  $\alpha^{ex}$  in SCF CO<sub>2</sub> is approximately equal to that in liquid CO<sub>2</sub> for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub>, respectively. The latter fact indicates that the rate constant for diffusion,  $k_{\text{diff}}$ , depends only on solvent viscosity,  $\eta$ , suggesting that the quenching in SCF  $CO_2$  can be interpreted in terms of the same framework as the Scheme 1 with the solvent cage effect.

Pressure Dependence of  $k_{\text{bim}}$  and the Contribution of Diffusion to the Quenching. The values of  $k_{\text{bim}}$  can be calculated by  $k_{\text{bim}} = k_{\text{bim}}^0 \gamma$ , and those of  $k_{\text{diff}}$  also reproduced using  $\alpha^{\text{ex}}$  (Table 3) and the solvent viscosity,  $\eta$ , according to eq 1. By using the values of  $k_{\text{bim}}$  and  $k_{\text{diff}}$ ,  $k_q$ (cal) is calculated by eq 16 (see eq 13).

$$k_{\rm q}({\rm cal}) = \frac{k_{\rm bim} k_{\rm diff}}{k_{\rm bim} + k_{\rm diff}}$$
(16)

The pressure dependences of  $k_{\text{bim}}$ ,  $k_{\text{diff}}$ ,  $k_{q}$ , and  $k_{q}$ (cal) thus calculated are shown in Figures 9 and 10 for DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub>, respectively. For DMEA/O<sub>2</sub> in SCF CO<sub>2</sub> (Figure 9a),  $k_{\text{diff}}$  is significantly larger than  $k_{\text{bim}}$  at pressures of 8.5 and 9.0 MPa, then close together, and their difference increases as pressure increases further. In liquid CO<sub>2</sub> and *n*-hexane (Figure 9, b and c),  $k_{\text{diff}}$  is close to  $k_{\text{bim}}$  at the lower pressure range and their difference increases with increasing pressure. These results



**Figure 10.** Pressure dependence of  $k_{diff}(\bigcirc)$ ,  $k_{bim}(\textcircled{\bullet})$ ,  $k_q(\triangle)$ , and  $k_q(cal)$ ( $\bigtriangledown$ ) for DMEA/CBr<sub>4</sub> in (a) SCF CO<sub>2</sub> at 35 °C, (b) liquid CO<sub>2</sub>, and (c) *n*-hexane at 25 °C.

indicate that the contribution of diffusion to the quenching is significant in both liquid and SCF  $CO_2$  in the pressure range examined.

For DMEA/CBr<sub>4</sub>, one can find similar observations as seen in Figure 10, but the difference between  $k_{\text{diff}}$  and  $k_{\text{bim}}$  is larger when compared to that for DMEA/O<sub>2</sub>. Therefore, the contribution of diffusion to the quenching is significant even in the lower pressure region. As a result, for both the systems of DMEA/O<sub>2</sub> and DMEA/CBr<sub>4</sub>, the quenching approaches the diffusioncontrolled rate in the higher pressure region since  $k_{\text{diff}}$  decreases whereas  $k_{\text{bim}}$  increases with increasing pressure.

#### Summary

It has been demonstrated that the fluorescence quenching by oxygen of 9,10-dimethylanthracene (DMEA) is not fully diffusion-controlled but competes with diffusion in the solvents with low viscosity by comparing the pressure and the pressureinduced solvent viscosity dependence of DMEA/O2 and DMEA/ CBr<sub>4</sub>. The analysis by eq 14 clearly reveals the contribution of diffusion to the quenching in DMEA/CBr<sub>4</sub> as well as in DMEA/  $O_2$ . The bimolecular rate constants for the quenching,  $k_{\text{bim}}$ , which increases with increasing the radial distribution function at the closest approach distance with the hard-sphere assumption, are found to be ca. 6  $\times$  10<sup>10</sup> and 1.2  $\times$  10<sup>11</sup> M<sup>-1</sup> s<sup>-1</sup> for DMEA/ O<sub>2</sub> and DMEA/CBr<sub>4</sub>, respectively, in both liquid CO<sub>2</sub> (25 °C, 10 MPa) and SCF CO<sub>2</sub> (35 °C, 8.5 MPa.). It has been shown that the observed quenching constant,  $k_q$ , is given by eq 16 using  $k_{\text{bim}}$  and  $k_{\text{diff}}$ . The latter is inversely proportional to the solvent viscosity,  $\eta$  (eq 1).

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(35) The radial distribution function at the closest approach distance,  $r_{M^*Q}$  (= $r_{M^*} + r_Q$ ) with the hard-sphere assumption,  $g(r_{M^*Q})$  is given by<sup>36</sup> eq A-1 ``

$$g(r_{M^*Q}) = \frac{1}{1-y} + \frac{3y}{(1-y)^2} \left(\frac{r_{red}}{r_s}\right) + \frac{2y^2}{(1-y)^3} \left(\frac{r_{red}}{r_s}\right)^2$$
(A-1)

where  $r_{\rm red} = r_{\rm M*} r_{\rm Q} / r_{\rm M*Q}$ , and y is the packing fraction, given in terms of the molar volume of solvent,  $V_{\rm S}$ , by eq A-2

$$y = \frac{4N_A \pi r_S^3}{3V_S} \tag{A-2}$$

By using the values of  $r_{\rm S}$ ,  $r_{\rm M^*}$ , and  $r_{\rm Q}$  listed in Table 2, together with the data of the solvent density,<sup>21–26</sup>  $g(r_{\rm M^*Q})$  was calculated by (A-1).

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